

# A Machine Learning Approach to Hand-Eye Calibration

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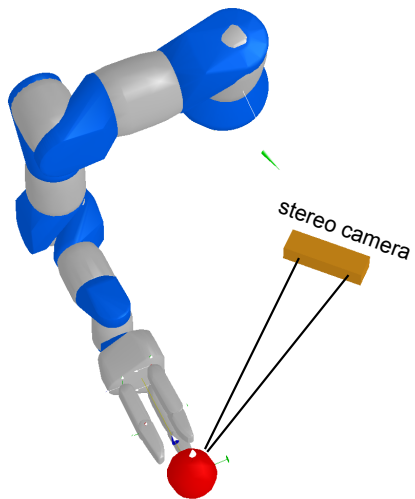
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# Introduction



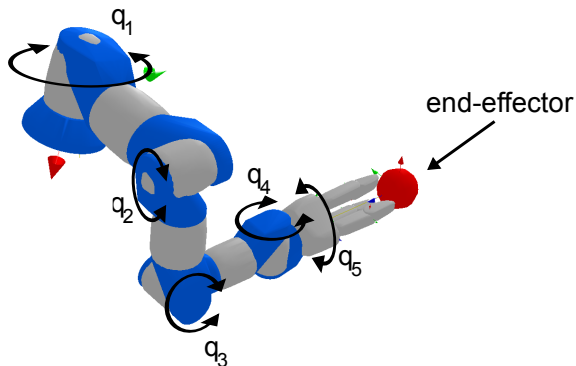
# Introduction

- ▶ pre-step to high level algorithms, e.g. object recognition or grasping
- ▶ calibrate each piece of hardware by itself
- ▶ after calibration measure relative offset between arm and camera (tricky)
- ▶ non-linearities, e.g. through distortions
- ▶ our idea: reformulation of these problems as a single problem
- ▶ simultaneously learn:
  - ▶ mapping from image coordinates to world coordinates
  - ▶ mapping from state vector  $q$  to world coordinates
- ▶ minimize error between both mappings

# Stand-alone Calibration: Robot Arm

## Forward Kinematics

- ▶  $n$ -dof robot arm:
  - ▶ controlled via state vector  $\vec{q} \in \mathbb{R}^n$ , e.g. joint angles
  - ▶ forward kinematics: given  $\vec{q}$  determine world coord.  $\vec{X}$  of end-effector
  - ▶ ideal world:  $\vec{X} = \omega(\vec{q})$ , actual world:  $\vec{X}_\delta = \omega(\vec{q} + \vec{\delta})$
  - ▶ unknown  $\vec{\delta}$  due to physical phenomena, e.g. cog wheels



# Stand-alone Calibration: Camera

## Pinhole Camera Model

- ▶ projection matrix  $P \in \mathbb{R}^{3 \times 4}$ :

$$P = KR[I | -\tilde{C}] \quad (1)$$

- ▶ projection of world point  $\vec{X} = (x, y, z, v)^t$  to image point  $\vec{x} = (u, v, w)$ :

$$\begin{pmatrix} u \\ v \\ w \end{pmatrix} = P \cdot \begin{pmatrix} x \\ y \\ z \\ v \end{pmatrix} \quad (2)$$

- ▶ intrinsics  $K \in \mathbb{R}^{3 \times 3}$ , extrinsics  $R \in \mathbb{R}^{3 \times 3}$ ,  $-\tilde{C} \in \mathbb{R}^3$ :

$$K = \begin{bmatrix} \alpha_x & s & x_0 \\ 0 & \alpha_y & y_0 \\ 0 & 0 & 1 \end{bmatrix}$$

# Stand-alone Calibration: Camera

Gold Standard algorithm<sup>1</sup> to determine int./ext. parameters

- ▶ solvable through Direct Linear Transform(ation) (DLT)
- ▶ given: collect  $n \geq 6$  point correspondances:  $\vec{x}_i \leftrightarrow \vec{X}_i$
- ▶ wanted: matrix  $P$ , so that

$$\vec{x}_i = P\vec{X}_i \Leftrightarrow \vec{x}_i \times (P\vec{X}_i) = \vec{0} \Leftrightarrow \vec{x}_i \times \begin{pmatrix} P^1\vec{X}_i \\ P^2\vec{X}_i \\ P^3\vec{X}_i \end{pmatrix} = \vec{0} \quad (3)$$

- ▶ rewrite eq. (3) in matrix notation,  $A \in \mathbb{R}^{12 \times 12}$ ,  $p \in \mathbb{R}^{12}$ :

$$A\vec{p} = \vec{0}, \text{ s.t. } \|\vec{p}\| = 1 \quad (4)$$

- ▶ solve with SVD:  $A = UDV^T$
- ▶  $p = V(:, \text{end})$ , if diagonal values of  $D$  in descending order

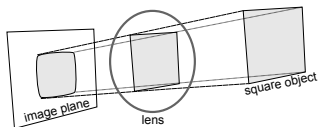
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<sup>1</sup>Zissermann, Multiple View Geometry

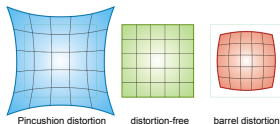
# Stand-alone Calibration: Camera

## Optical Aberration/Distortion

- ▶ camera with lens  $\neq$  pin-hole camera model (!)
  - ▶ distortion (radial, tangential, ...)
  - ▶ significance increases while focal length (and price) decreases



(a) lens distortion



(b) types of (radial) distortion



# Stand-alone Calibration: Camera

## Optical Aberration/Distortion

- ▶ correction of radial distortion

$$x' = x(1 + k_1r^2 + k_2r^4 + k_3r^6)$$

$$y' = y(1 + k_1r^2 + k_2r^4 + k_3r^6)$$

- ▶ correction of tangential distortion

$$x' = x + [2p_1y + p_2(r^2 + 2x^2)]$$

$$y' = y + [p_1(r^2 + 2y^2) + 2p_2x]$$

- ▶ minimizing geometric error of a calibration object (chessboard) based on deviation from linear mappings

# Stand-alone Calibration: Camera

## Stereo Calibration

- ▶ first, single-camera calibration to obtain

$$P_l = K_l R_l [I | -\tilde{C}_l]$$

and

$$P_r = K_r R_r [I | -\tilde{C}_r]$$

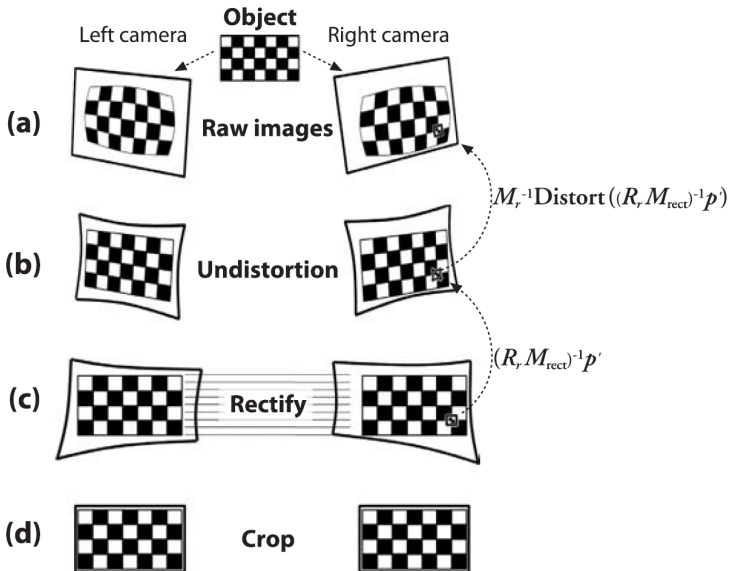
- ▶ then, translation matrix  $R$  and translation  $T$  from right to left camera coordinate system:

$$\begin{aligned} R &= R_r (R_l)^T \\ T &= \tilde{C}_r - R \tilde{C}_l \end{aligned}$$

(5)

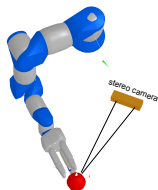
# Stand-alone Calibration: Camera

## Calibration Pipeline



# Hand-Eye Calibration

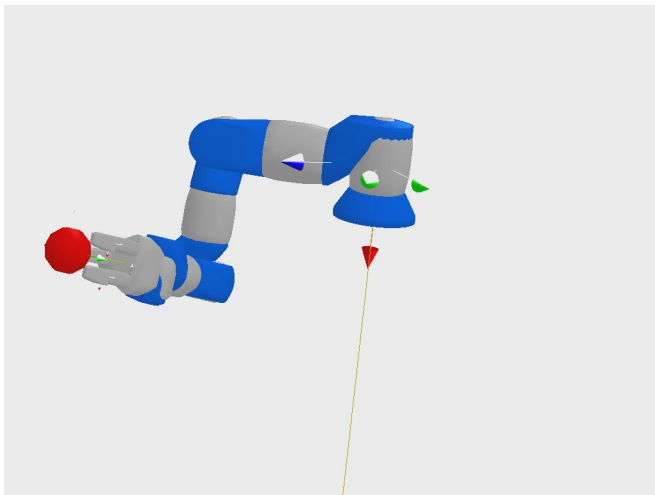
## General Setup



- ▶ unknown calibrations parameters: initially, hardware is uncalibrated!
- ▶ unknown rotation & translation between robot and camera
- ▶ fiducial marker (“lolly pop”) in robot’s hand
- ▶ visually track lolly pop and record image coordinates  $\vec{x}_i^l$  and  $\vec{x}_i^r$
- ▶ record state vector  $\vec{q}_i$  of robot
- ▶ ...

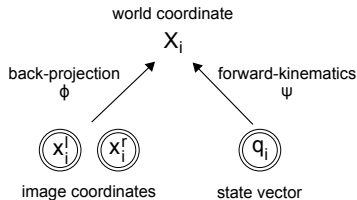
# Hand-Eye Calibration

## Data Acquisition



# Hand-Eye Calibration

## Minimization Problem



- ▶ given: set of image points  $\vec{x}_i^l, \vec{x}_i^r$ , and state vectors  $\vec{q}_i$
- ▶ wanted: world coordinates  $\vec{X}_i$  from non-linear mappings, such that

$$\Phi(\vec{x}_i^l, \vec{x}_i^r) = \vec{X}_i = \psi(\vec{q}_i) \quad (6)$$

# Hand-Eye Calibration

## Minimization Problem

- ▶ global cost function:

$$L_{\text{global}} = \sum_i |\psi(\vec{q}_i) - \Phi(\vec{x}_i^l, \vec{x}_i^r)|^2 \quad (7)$$

- ▶ hard to minimize eq. (7) directly
- ▶ local cost function for image points:

$$L_{\vec{x}} = \sum_i |X_i - \Phi(\vec{x}_i^l, \vec{x}_i^r)|^2 \quad (8)$$

- ▶ local cost function for state vector:

$$L_{\vec{q}} = \sum_i |X_i - \psi(\vec{q}_i)|^2 \quad (9)$$

# Hand-Eye Calibration

## Suggested Algorithm

**Input:** image point pairs  $(\vec{x}_i^l, \vec{x}_i^r)$ , state vectors  $\vec{q}_i$

**Output:** mappings  $\psi(\vec{q}_i)$  and  $\Phi(\vec{x}_i^l, \vec{x}_i^r)$

- 1: define  $\psi'(\cdot)$  as regular forward kinematics
- 2: **repeat**
- 3:   learn  $\Phi'(\cdot)$  given  $\psi'(\vec{q}_i)$  (eq. (8))
- 4:   learn  $\psi'(\cdot)$  given  $\Phi'(\vec{x}_i^l, \vec{x}_i^r)$  (eq. (9))
- 5: **until**  $L_{\text{global}} < \varepsilon$
- 6: **return**  $\Phi = \Phi', \psi = \psi'$



# Hand-Eye Calibration

## Learning Step

- ▶ SVM regression
- ▶ Gaussian Process
- ▶ Multi-layer Perceptron
- ▶ [your algorithm]
- ▶ ...

## Next steps

- ▶ Proof of concept in simulator
- ▶ Verification with actual camera and arm
- ▶ make data available to IDA members
- ▶ ...

# Conclusions

- ▶ iterative approach to the Hand-Eye calibration problem
- ▶ solving problem in “EM-fashion”
- ▶ no assumption on parameters
- ▶ no need to measure exact camera-to-robot offset
- ▶ interesting for people with algorithm but no data/problem

**10q!**  
Questions?